

**ISO/TS 21748: A new guide to uncertainty estimation using interlaboratory study data**

S Ellison  
LGC

/Eurachem-UK/1

---

---

---


---

---

---

---

---



**Overview**

- Reproducibility and uncertainty estimation
- Introduction to ISO TS 21748

/Eurachem-UK/2

---

---

---


---

---

---

---

---



**What is Measurement Uncertainty?**

“A parameter, associated with the result of a measurement, that characterises the dispersion of the values that could reasonably be attributed to the measurand”  
*(ISO Guide)*

**The number after the ±**

/Eurachem-UK/3

---

---

---

---

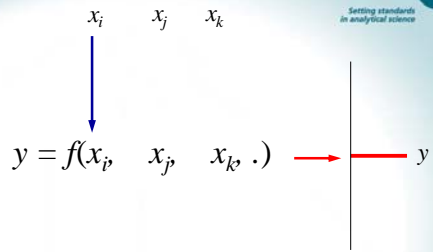
---

---

---

---

## Models and Uncertainty



/Eurachem-UK/4

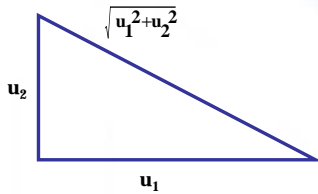
## ISO Guide approach



- Specify the measurand
  - including complete equation
- Quantify significant uncertainties in all parameters
  - A: from statistics of repeated experiment
  - B: by any other means (theory, certificates, judgement...)
- Express as standard deviation
- Combine according to stated principles

/Eurachem-UK/7

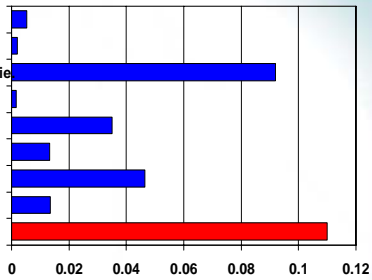
## Combining uncertainties (ISO)



- *Standard deviations*
- *Established error propagation theory*

/Eurachem-UK/8

Oxidant conc.  
Extent Oxid<sup>4</sup>4ie



/Eurachem-UK/9



/Eurachem-UK'10

## A simpler model



- The best available estimate of precision
  - *An effect varied representatively during a precision experiment requires no further study*
- The best available estimate of bias *and its uncertainty*
- Other significant effects evaluated
  - By experiment, or from standing data

/Eurachem-UK/13

---

---

---

---

---

---

---

---

## Collaboratively trialed methods



- Collaboratively trialed method
  - bias and precision verified in-house
- Assessed against collaborative study estimates
  - ISO/TS 21748
  - demonstrate method bias and repeatability are under control

/Eurachem-UK/14

---

---

---

---

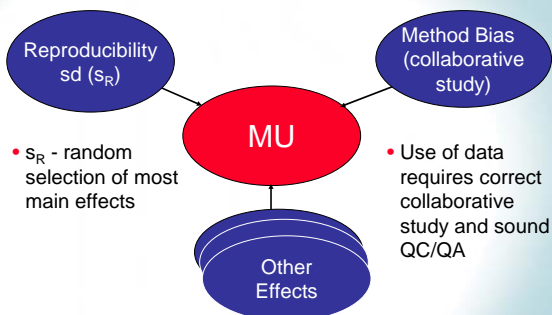
---

---

---

---

## Collaborative trial data



/Eurachem-UK/15

---

---

---

---

---

---

---

---

## Process for evaluating uncertainty according to ISO/TS 21748



- Obtain repeatability, reproducibility and bias estimates from collaborative study
- Establish whether laboratory bias is within that expected on the basis of the collaborative study
- Establish whether laboratory precision is within that expected on the basis of the collaborative study
- Where laboratory bias and precision are under control, combine effects appropriately to form a combined uncertainty estimate

/Eurachem-UK/16

---

---

---

---

---

---

---

---

## TS21748 uncertainty budget



$$u_c^2(y) = \hat{s}_R^2 + u^2(\hat{\phantom{y}}) + \sum_{i=k,n} c_i^2 u^2(x_i)$$

- Combined uncertainty
  - Adjusted reproducibility estimate
    - Uncertainty associated with method bias
      - Effects not covered, e.g. sampling uncertainty

/Eurachem-UK/17

---

---

---

---

---

---

---

---

## Demonstrating acceptable laboratory bias



- Study of CRMs
  - Simple test for significant bias
  - Ideally with small bias check uncertainty
- Comparison with known test method
  - Typically paired tests on several materials
- Comparison with other laboratories
  - Proficiency testing or other collaborative study

/Eurachem-UK/18

---

---

---

---

---

---

---

---

## Including trueness data in an uncertainty estimate

$$u_c^2(y) = \hat{s}_R^2 + u^2(\hat{\phantom{y}}) + \sum_{i=k,n} c_i^2 u^2(x_i)$$

- Combined uncertainty
- Adjusted reproducibility estimate
- **Uncertainty associated with method bias**
  - Effects not covered, e.g. sampling uncertainty

/Eurachem-UK/19

## Demonstrating acceptable laboratory precision

•

/Eurachem-UK/20

### Including reproducibility data

Setting standards in analytical science **LGC**

$$u_c^2(y) = \hat{s}_R^2 + u^2(\hat{\phantom{y}}) + \sum_{i=k,n} c_i^2 u^2(x_i)$$

- Combined uncertainty
- **Adjusted reproducibility estimate**
  - Uncertainty associated with method bias
  - Effects not covered, e.g. sampling uncertainty

/Eurachem-UK/22

---

---

---

---

---

---

---

---

### Other effects

Setting standards in analytical science **LGC**

- Simple “worst case” calculations can often show an effect is negligible
- Formal uncertainty calculations often show negligible components
- Typical criteria:
  - $u < u_{\max}/3$  (<6% effect on combined uncertainty)
  - $u < u_{\max}/5$  (<2% effect on combined uncertainty)
  - ISO/TS 21748 effects  $< 0.2S_R$

/Eurachem-UK/23

---

---

---

---

---

---

---

---

### Numerical calculation

Setting standards in analytical science **LGC**

Calculated result  $y$

$y(x+u(x))$   
 $y(x)$

$x$   $x+u(x)$

$u(y) \approx y(x+u(x)) - y(x)$

/Eurachem-UK/24

---

---

---

---

---

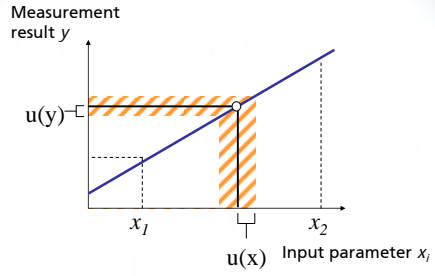
---

---

---



## Other effects: A simple uncertainty experiment



/Eurachem-UK/25